Diffusion in Concert halls analyzed as a function of time during the decay process

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Agenda

- Why investigate diffusivity?
- Directional Diffusion and Steady State Diffusivity
- Defining the Dynamic Diffusion Curve (DDC)
- Normalising the DDC
- Typical features of the DDC
- DDC in (models of) 12 concert halls
- DDC as a function of distance in 2 halls
- DDC and flutter echo
- Conclusions

Motivation, why investigate diffusivity?

- Diffusivity is assumed to be important for the quality of concert halls
- Efforts are put into promoting diffuse reflections;
  - making surfaces scatter sound
  - shape of geometry
  - distribution of materials

Therefore we should understand better how given designs affect diffusivity in rooms.

Steady State Diffusivity

Thiele (1953) defined Directional Diffusion (d in %) as

$$d = (1 - \frac{\mu}{\mu_0}) \times 100\% = \frac{E - I}{E} \times 100\%$$

where E is sound energy and I is sound intensity

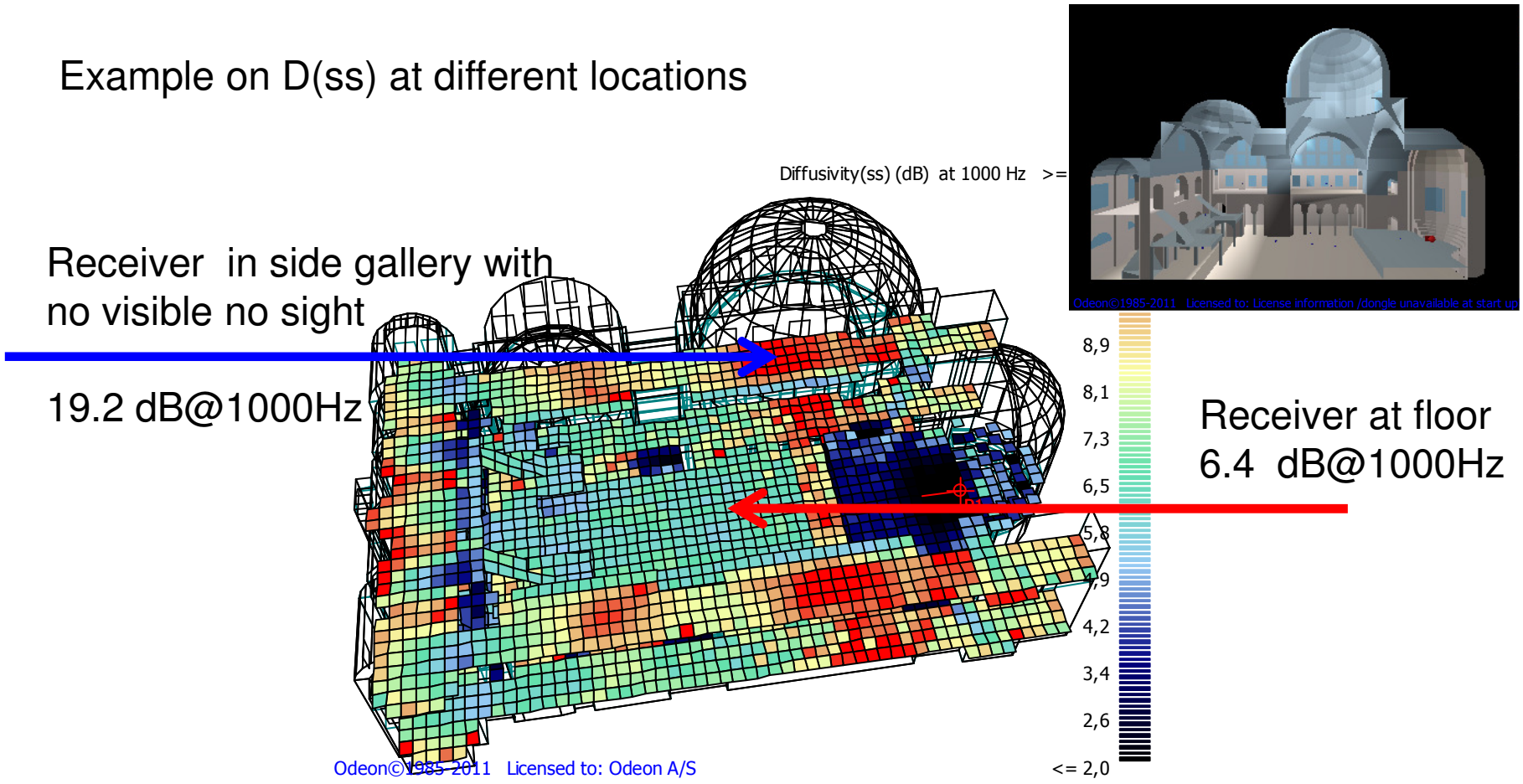
*D*irectional *D*iffusion is usually close to 100%, so instead we may prefer to define *S*teady *S*tate *D*iffusivity in dB as:

$$D(ss) = 10 \times \log_{10}(E) - 10 \times \log_{10}(I) \qquad [\mathrm{dB}]$$

Note! $I = \sqrt{I_{8x}^2 + I_{8x}^2 + I_{8z}^2}$

Steady State Diffusivity

Example on D(ss) at different locations



Receiver in side gallery with no visible no sight

19.2 dB@1000Hz

Receiver at floor

6.4 dB@1000Hz

Dynamic Diffusivity Curve – DDC energy and intensity curves

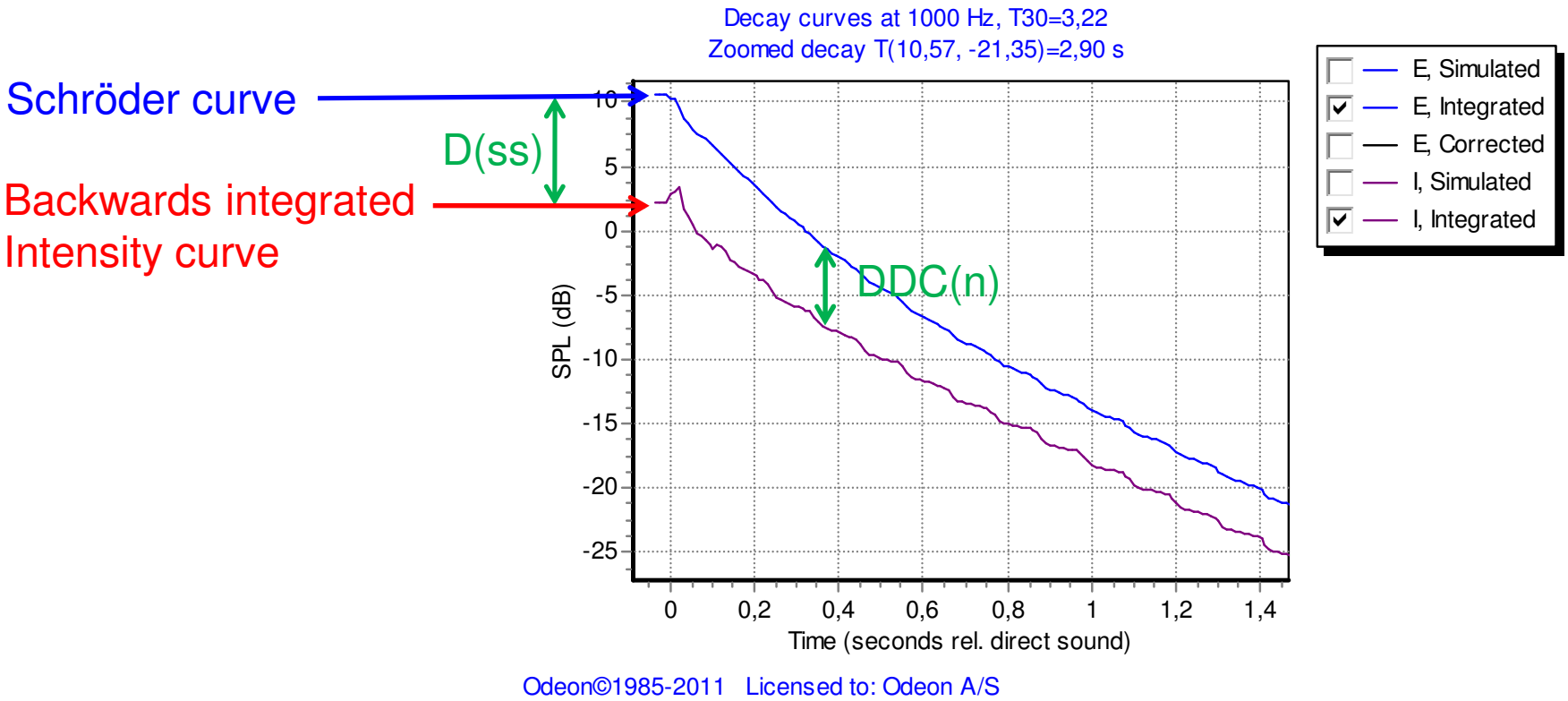
Backwards integrated squared impulse response curve

$$E(t_n) = 10 \times \log_{10} \int_{t=\infty}^{t=t_n} E(t)\, dt \qquad [dB]$$

Backwards integrated intensity curve

$$I(t_n) = 10 \times \log_{10} \sqrt{\left(\int_{t=\infty}^{t=t_n} I(t)_{8x}\, dt\right)^2 + \left(\int_{t=\infty}^{t=t_n} I(t)_{8y}\, dt\right)^2 + \left(\int_{t=\infty}^{t=t_n} I(t)_{8z}\, dt\right)^2}$$

Dynamic Diffusivity Curve – DDC example; energy and intensity curves



Dynamic Diffusivity Curve – DDC

DDC is the difference between energy and intensity curves

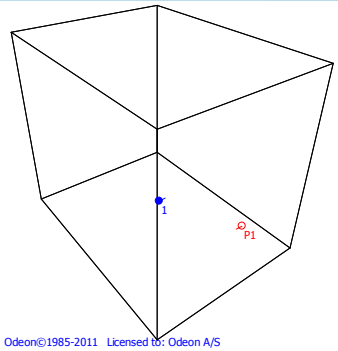
$$DDC(n) = E(n) - I(n)$$

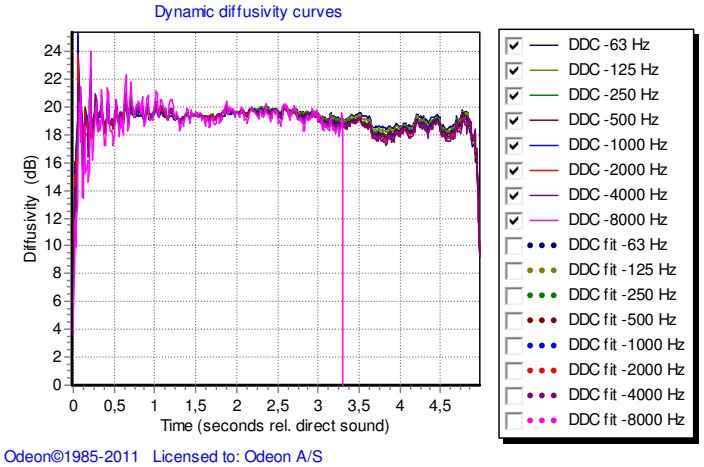
$$= 10 \times \log_{10} \int_{t=\infty}^{t=t_n} E(t)\, dt$$

$$- 10 \times \log_{10} \sqrt{\left(\int_{t=\infty}^{t=t_n} I(t)_{8x}\, dt\right)^2 + \left(\int_{t=\infty}^{t=t_n} I(t)_{8y}\, dt\right)^2 + \left(\int_{t=\infty}^{t=t_n} I(t)_{8z}\, dt\right)^2} \quad [\mathrm{dB}]$$

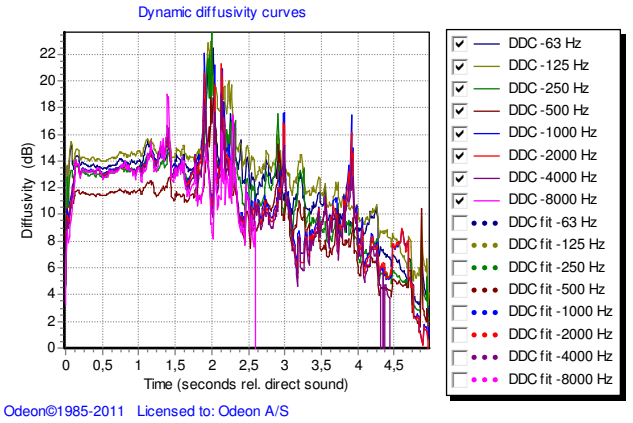
Comparing DDC for rooms with different T30

Box shaped room 12 x 14 x 16





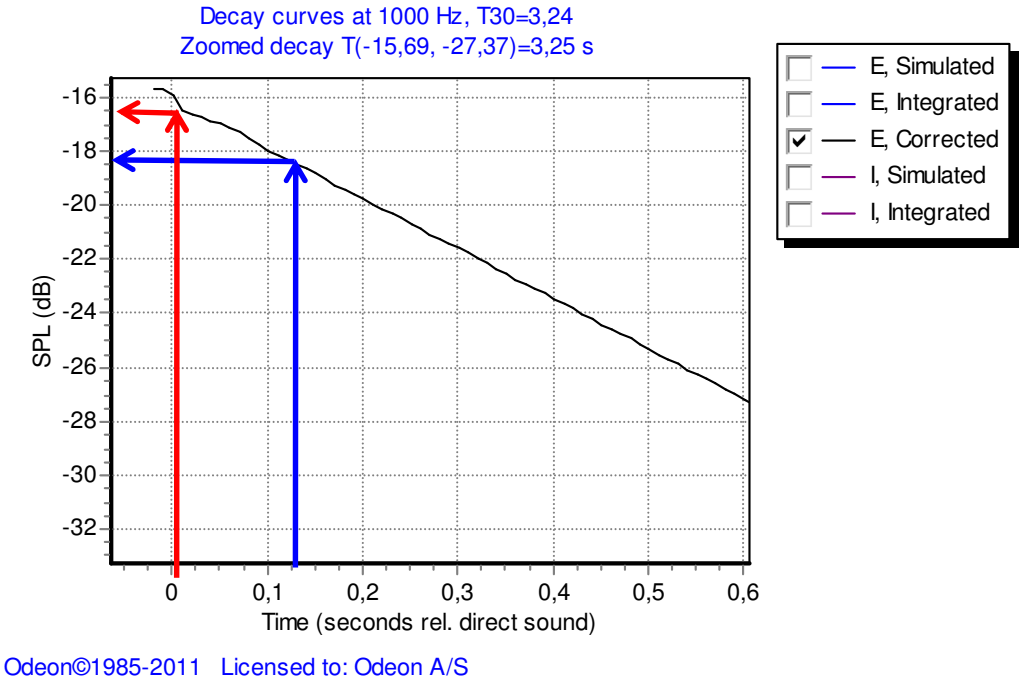
T30=3.24s@1000 Hz
All hard surfaces
Low scattering



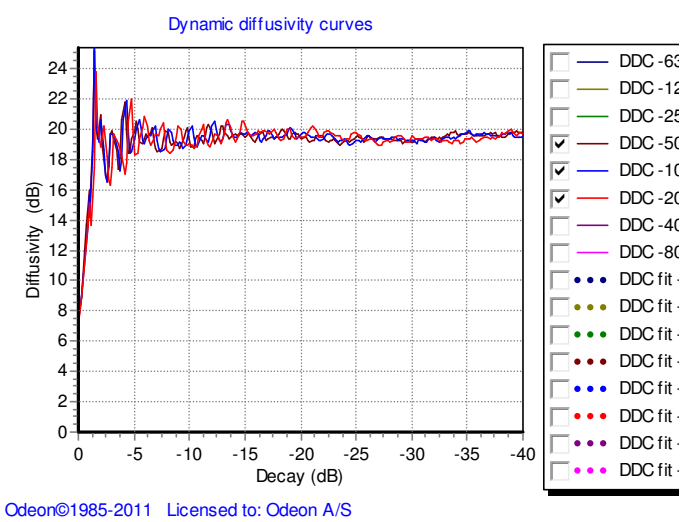
T30=1.65s@1000 Hz
hard surfaces+absorbing ceiling
High scattering

Normalising DDC

- Use Schröder curve for normalization
- Substitute time axis with decay [dB]



Normalising DDC



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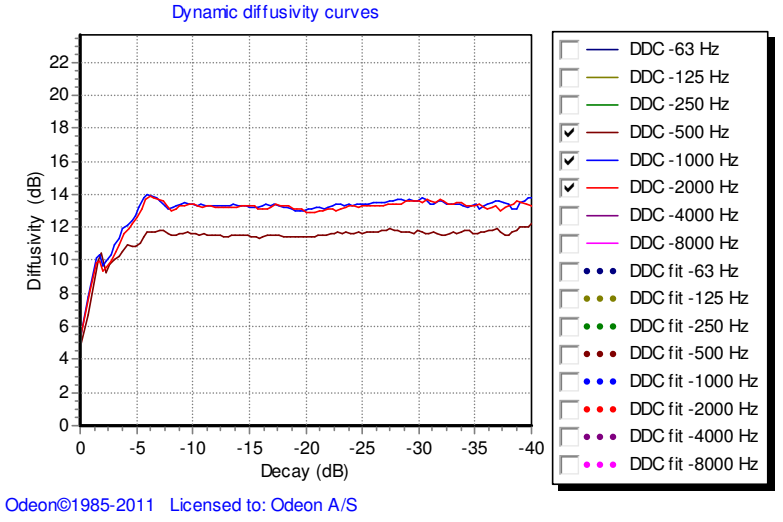
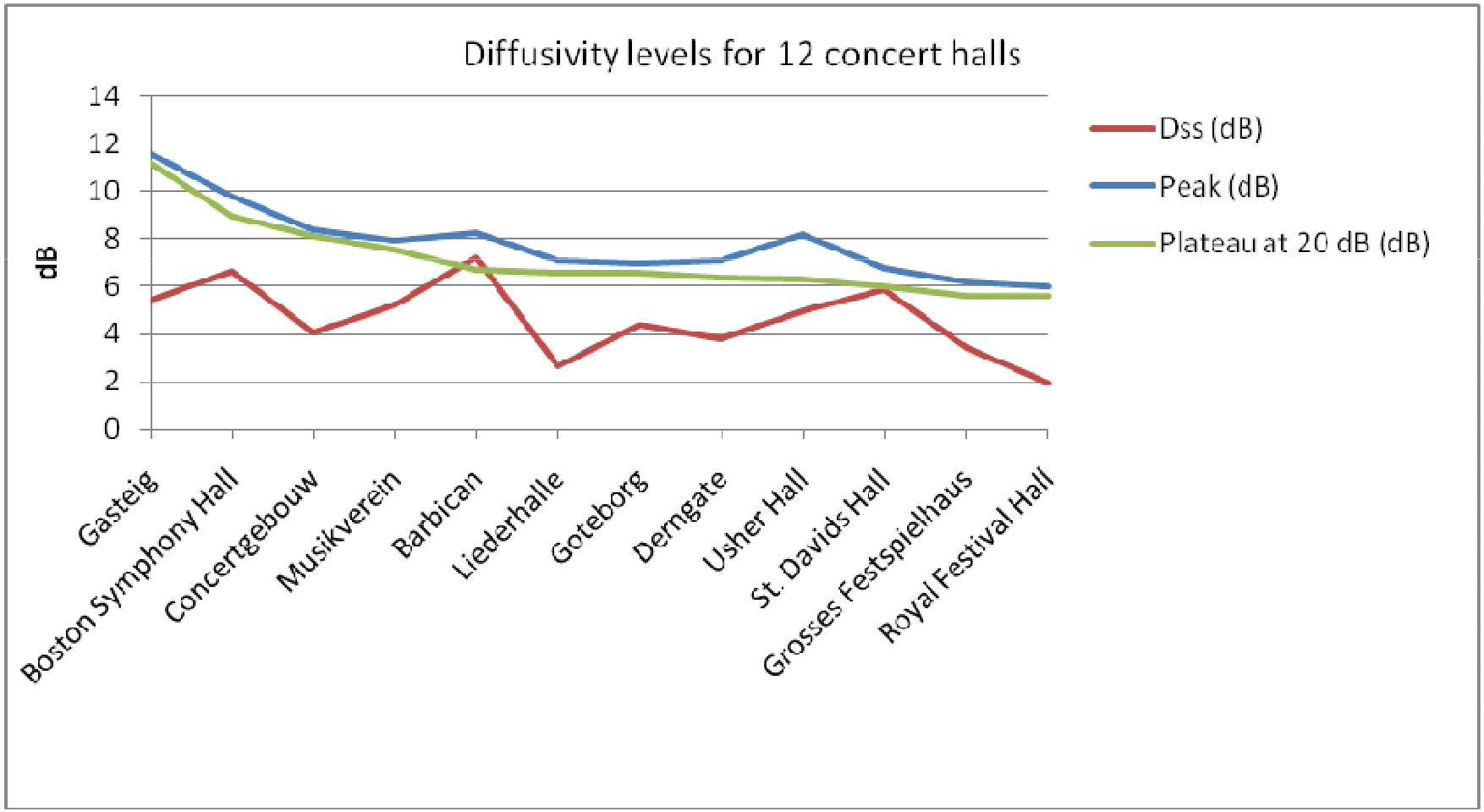


T30=1.65s@1000 Hz
hard surfaces+absorbing ceiling
High scattering

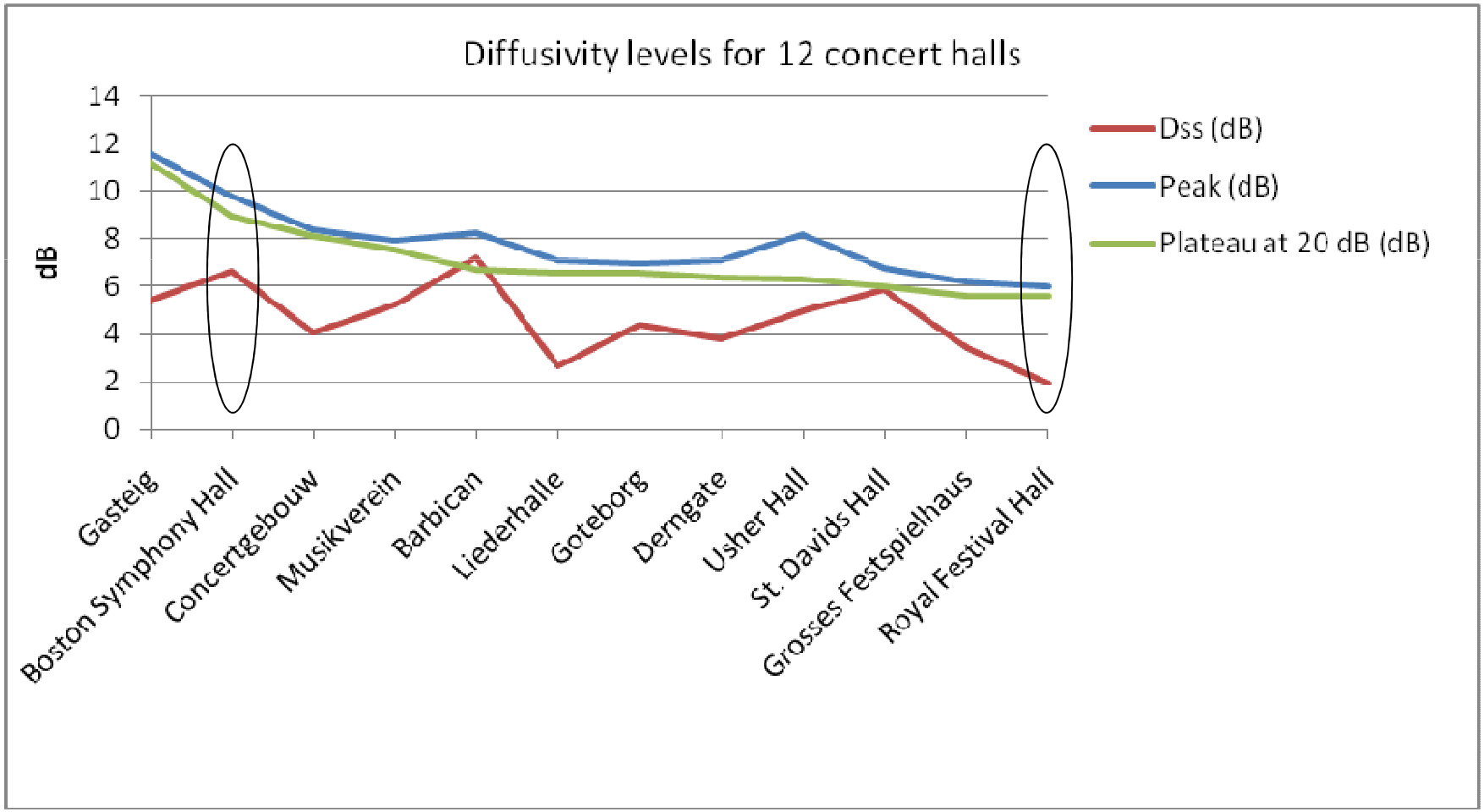
Typical features of DDC

- Initial value Dss is lower that later values
- A peak appears within the first 5 (to 10) dB
- DDC reaches its plateau level after some 5 to 10 dB decay
- The plateau can have ripples e.g. in case of a flutter echo

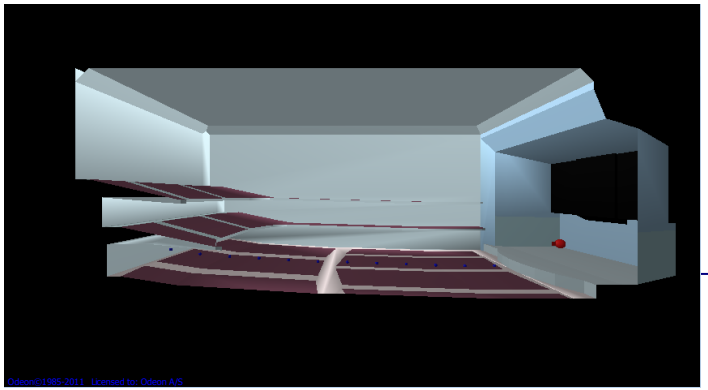
12 Concert halls (models)
Source mid stage – receiver mid-parterre
Dss, Peak and Plateau levels



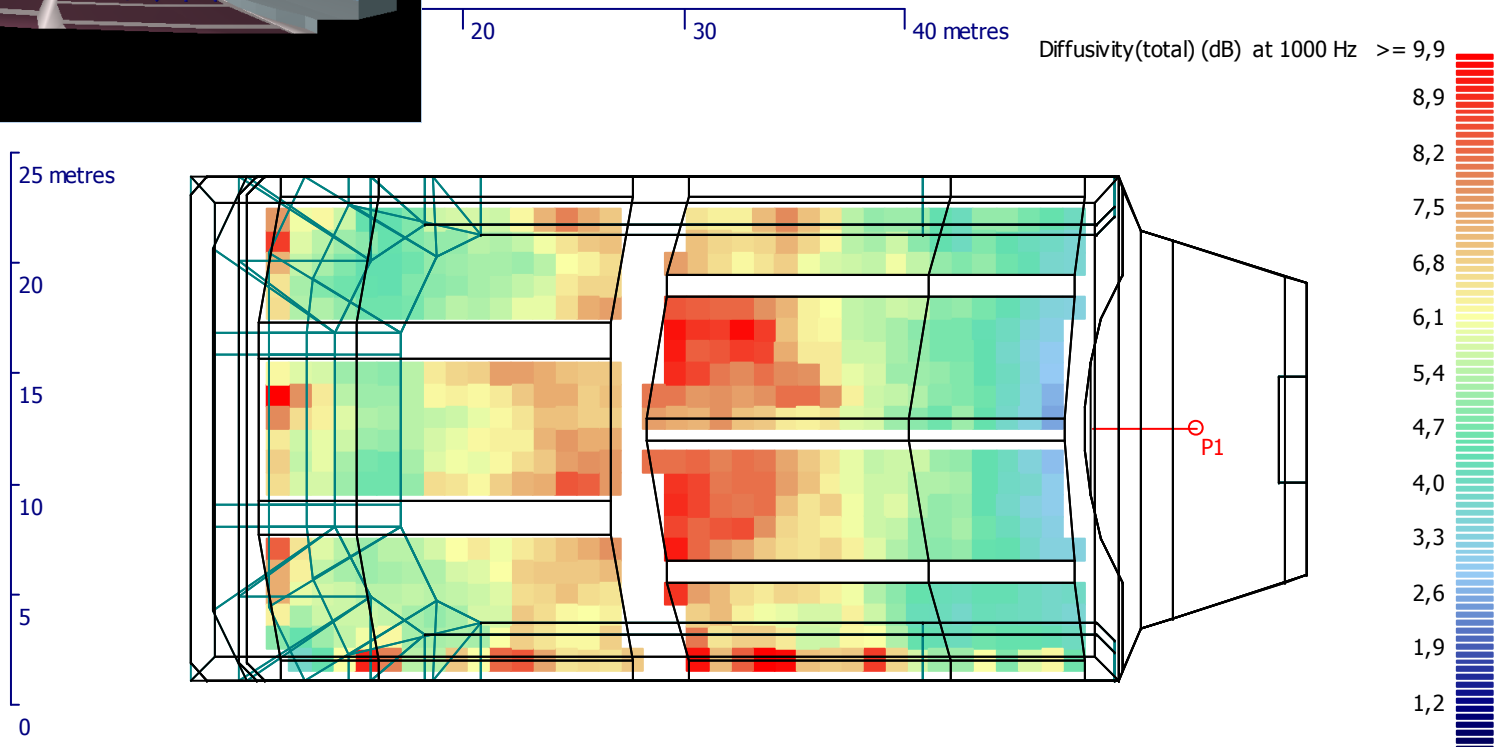
Two examples for comparison



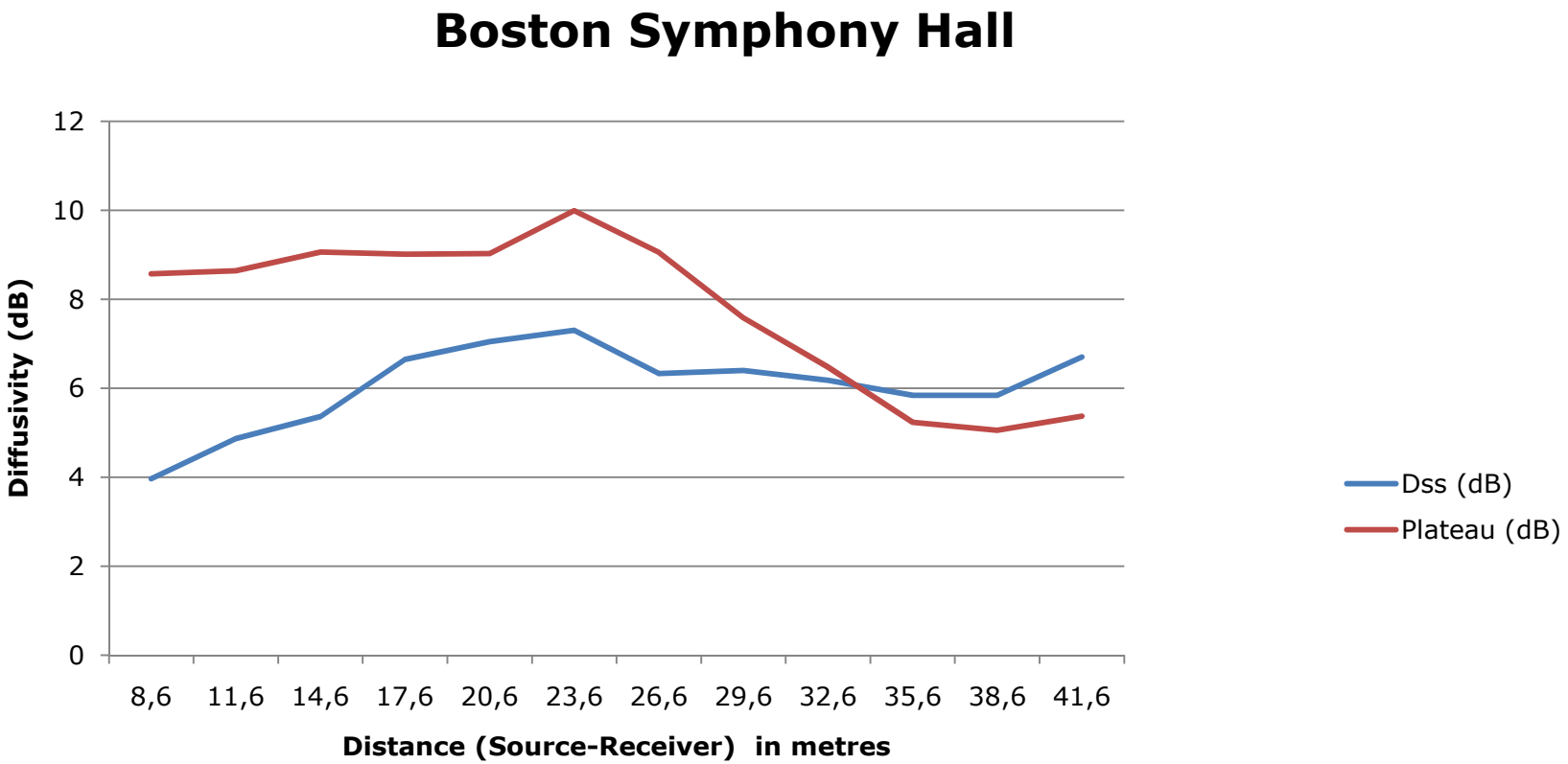
Diffusivity(Dss) – Boston Symphony Hall



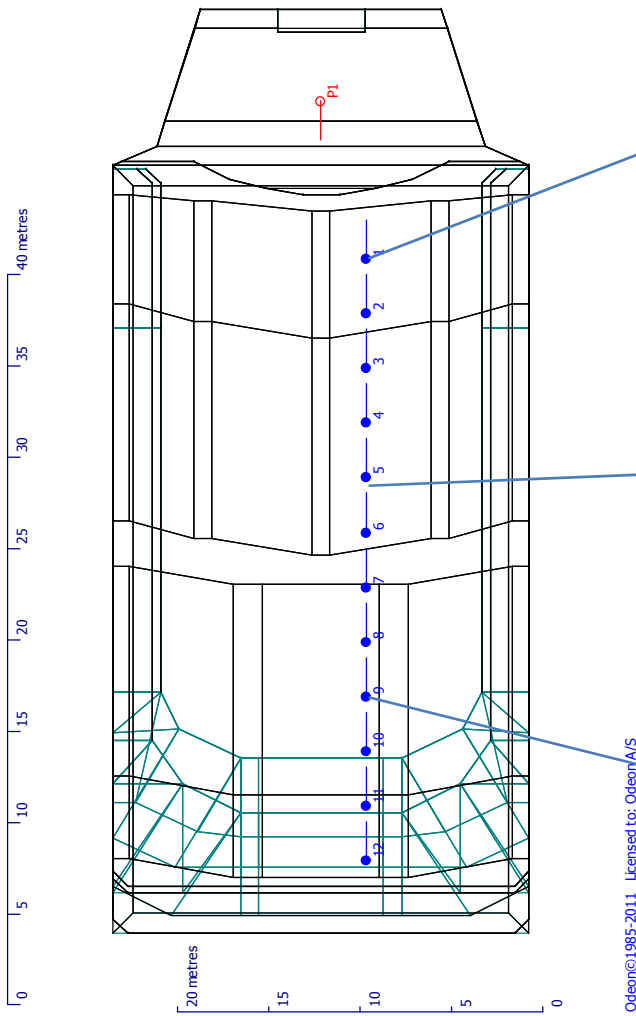
Floor level, only

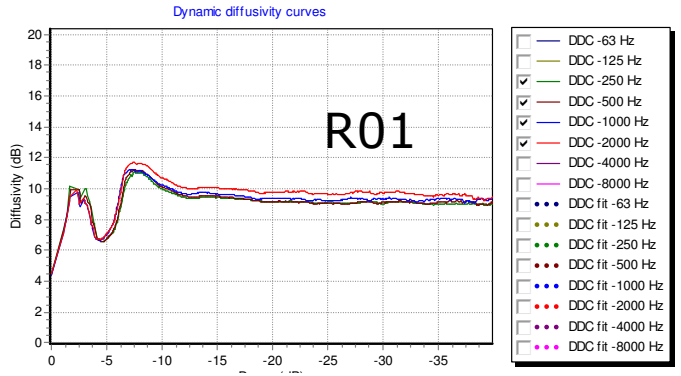


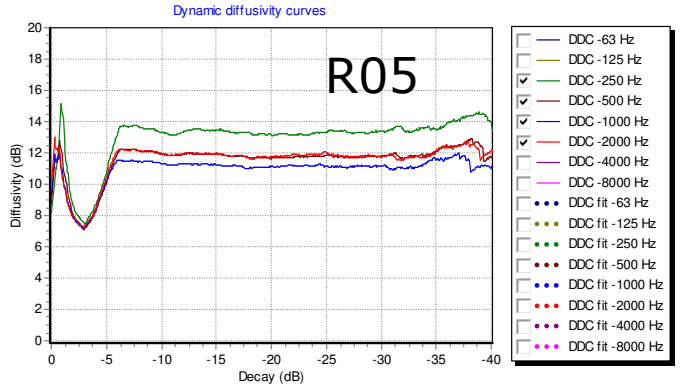
Dss and Plateau levels as a function of distance

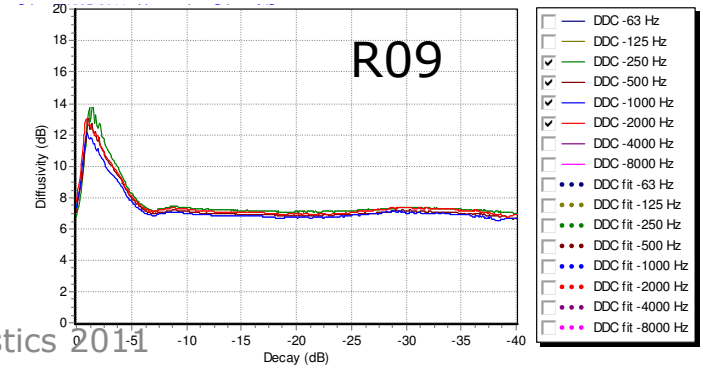


DDC variation with distance in BSH

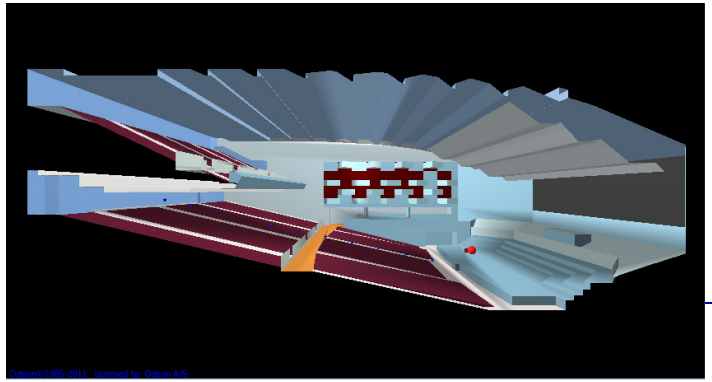




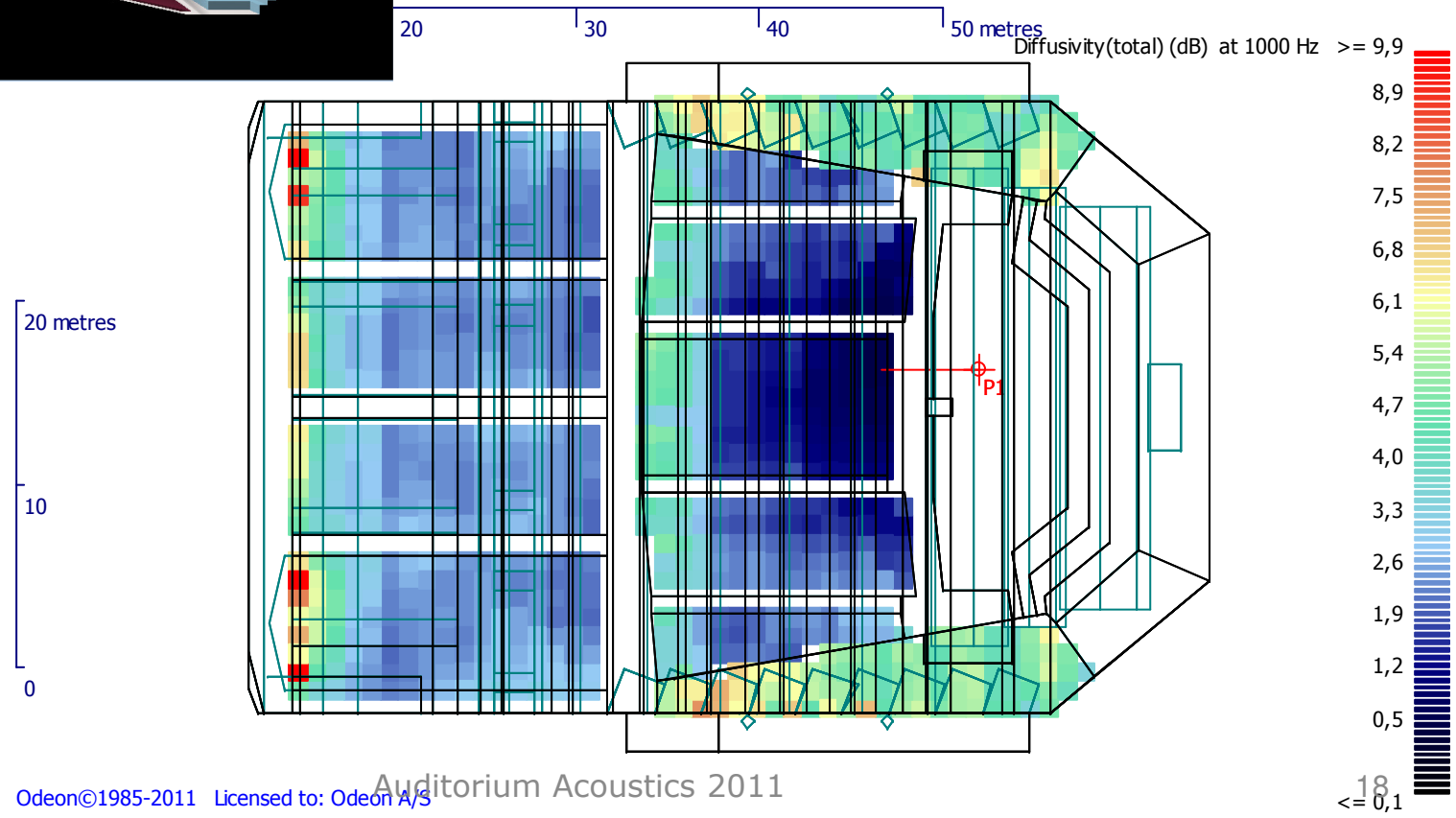




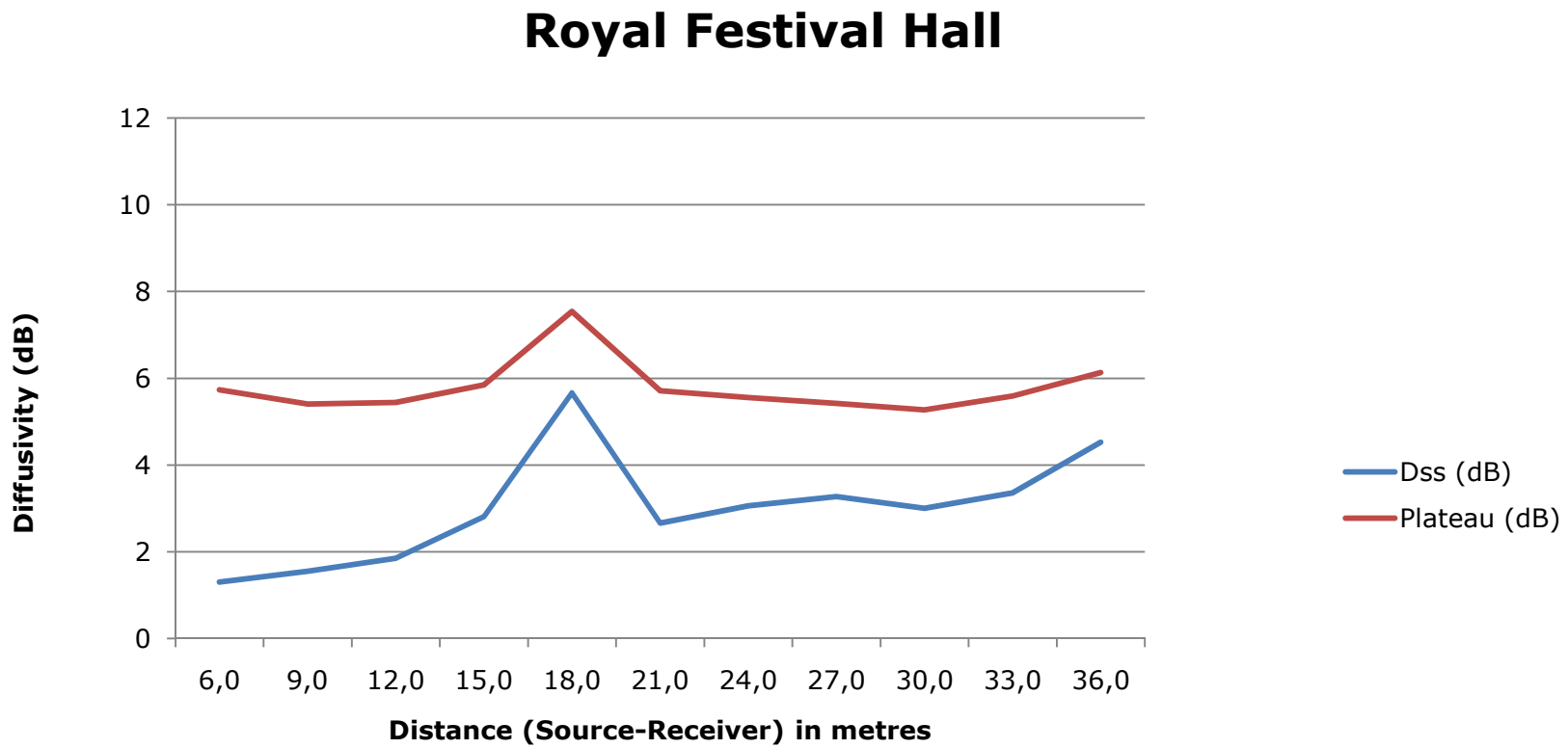
Diffusivity(Dss) – Royal Festival Hall



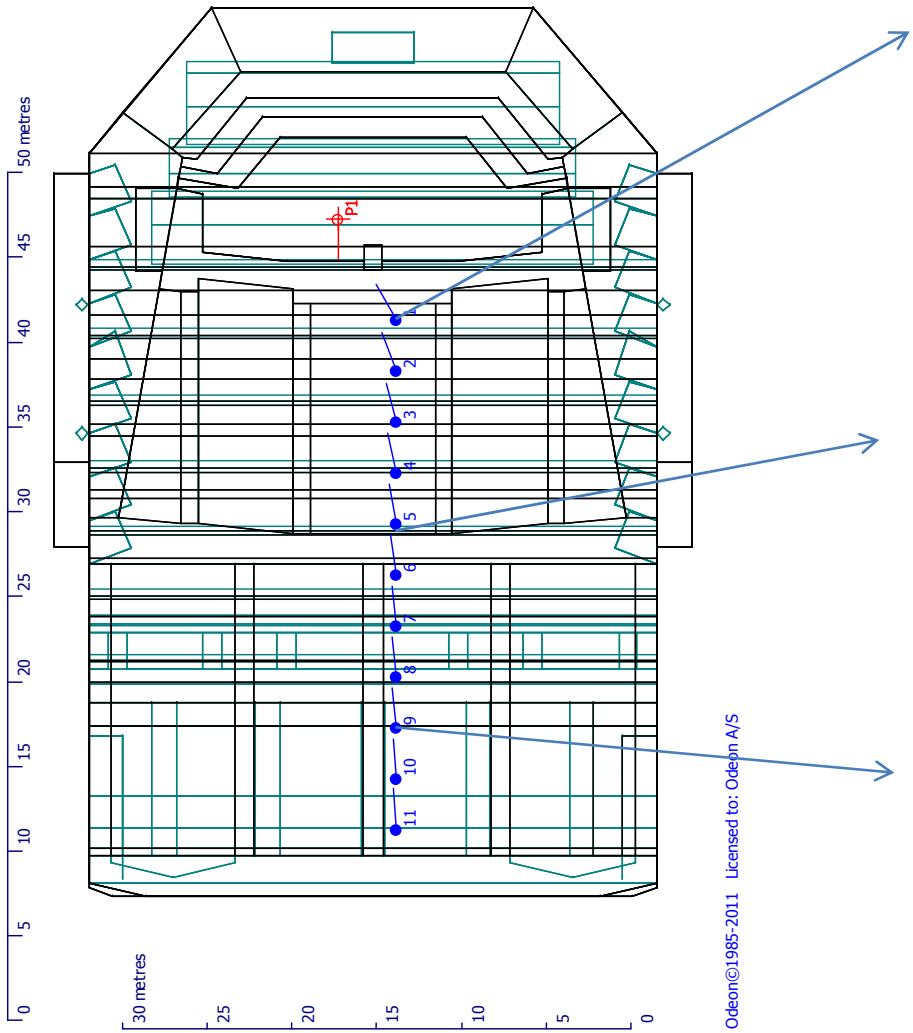
Floor level, only

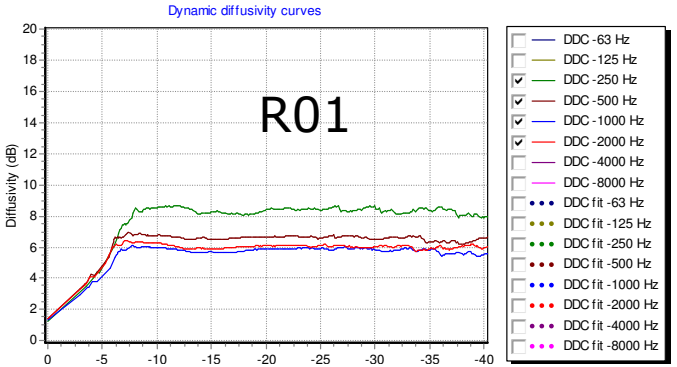


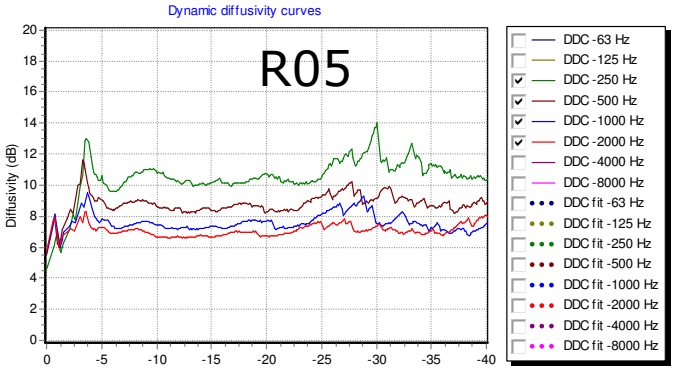
Dss and Plateau levels as a function of distance

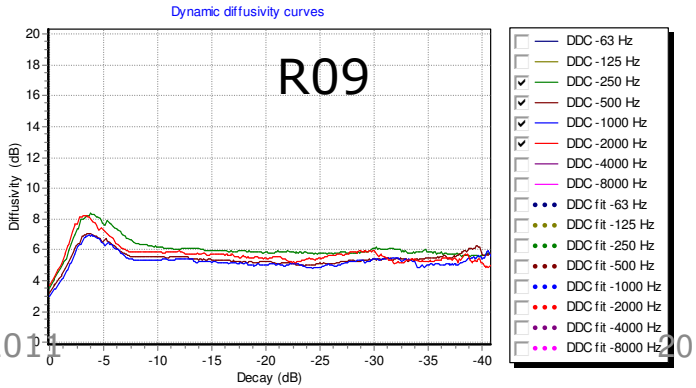


DDC variation with distance in RFH



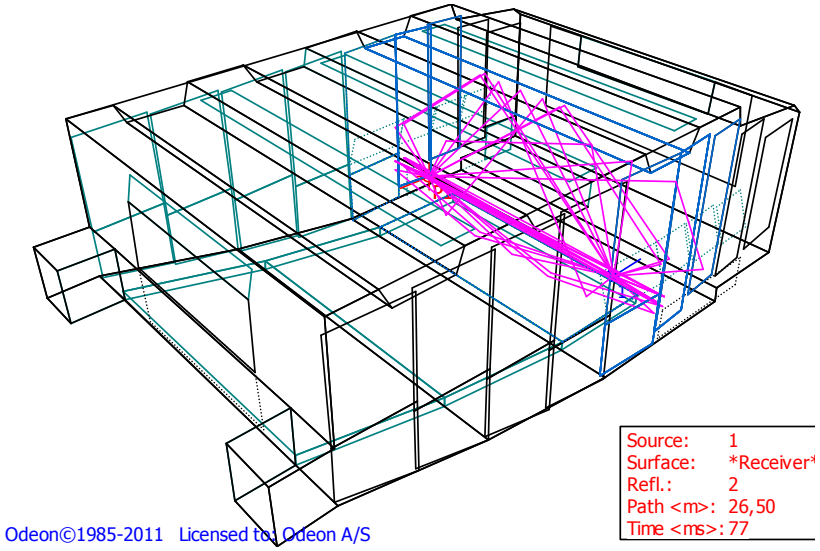




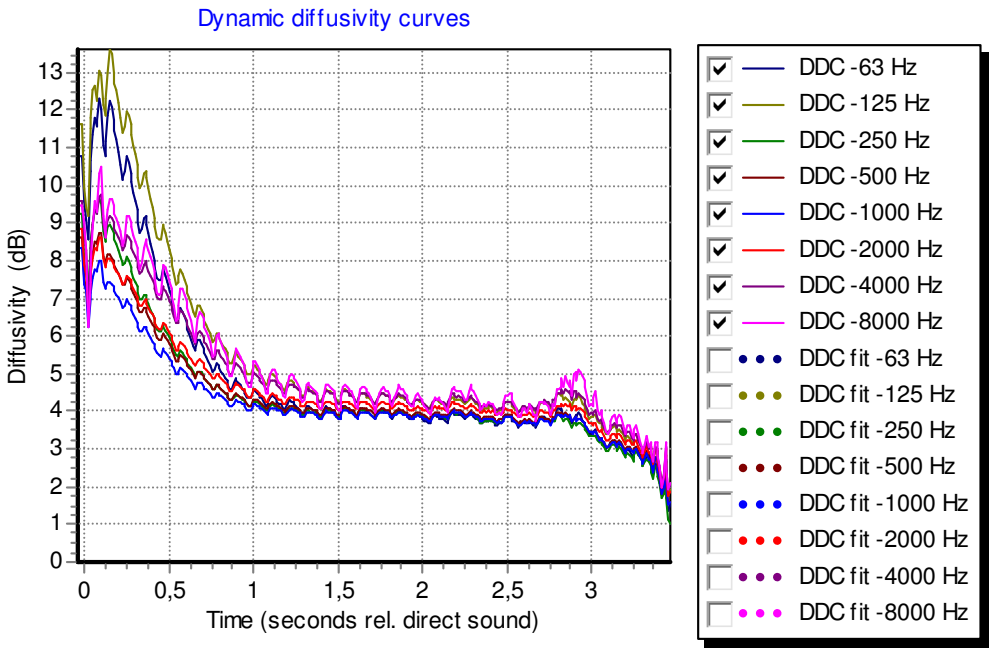


DDC and Flutter Echo

Queen's Hall, Copenhagen



4 reflector panels tilted slightly inwards – creating a flutter echo



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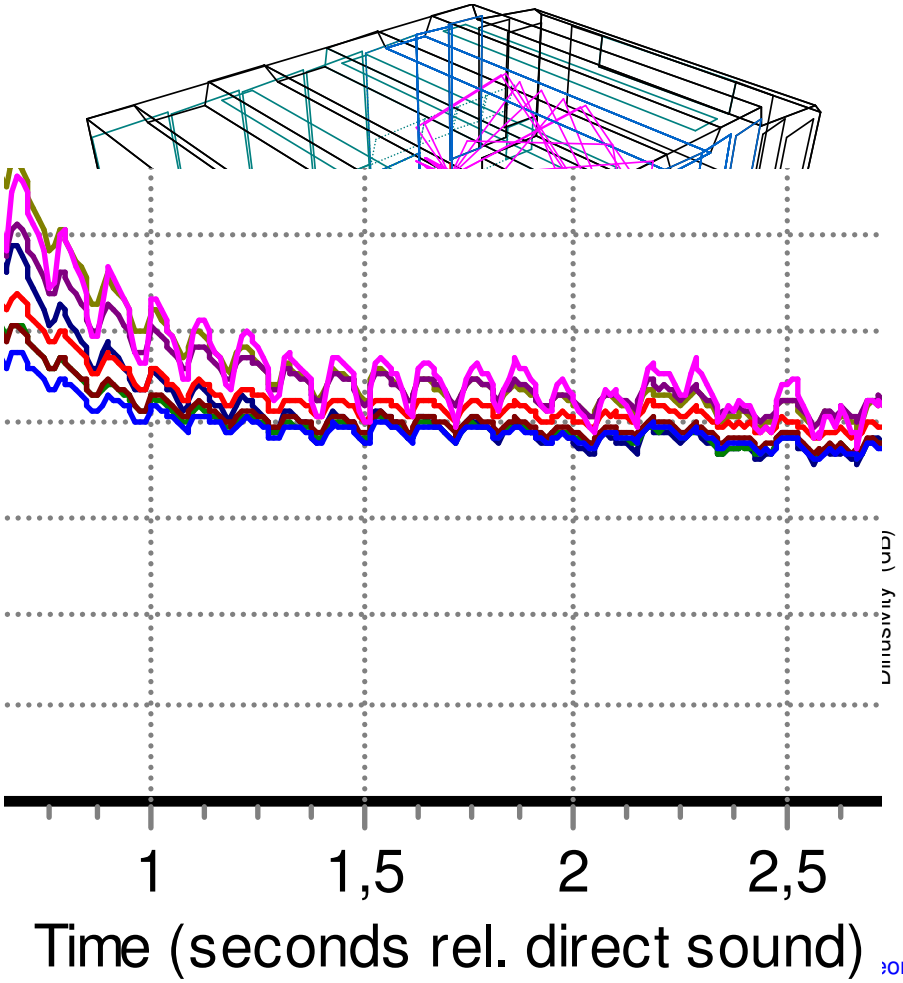

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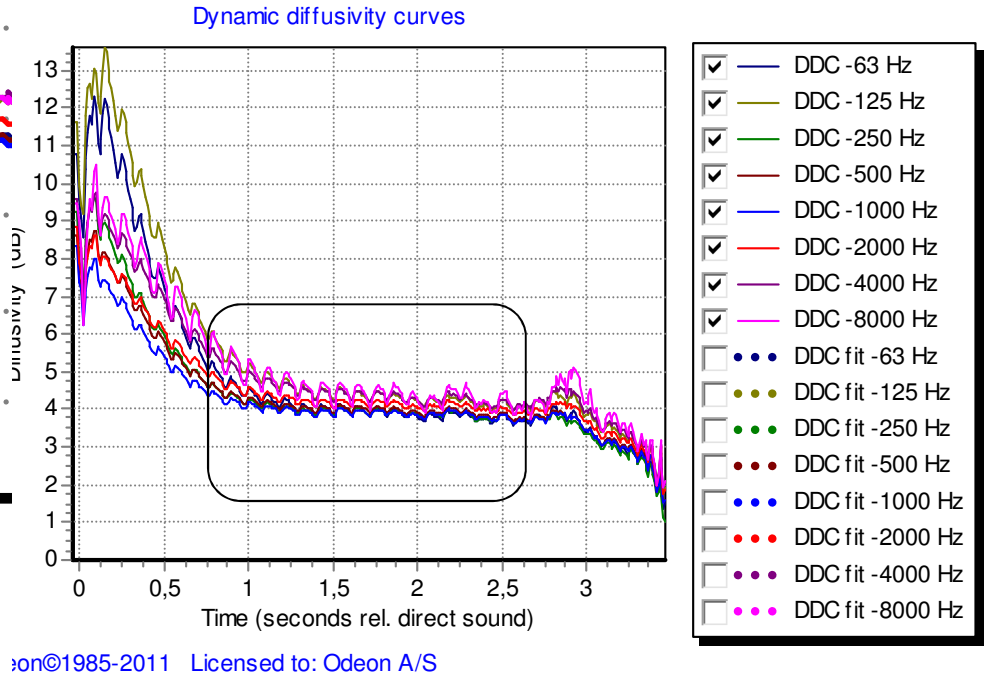
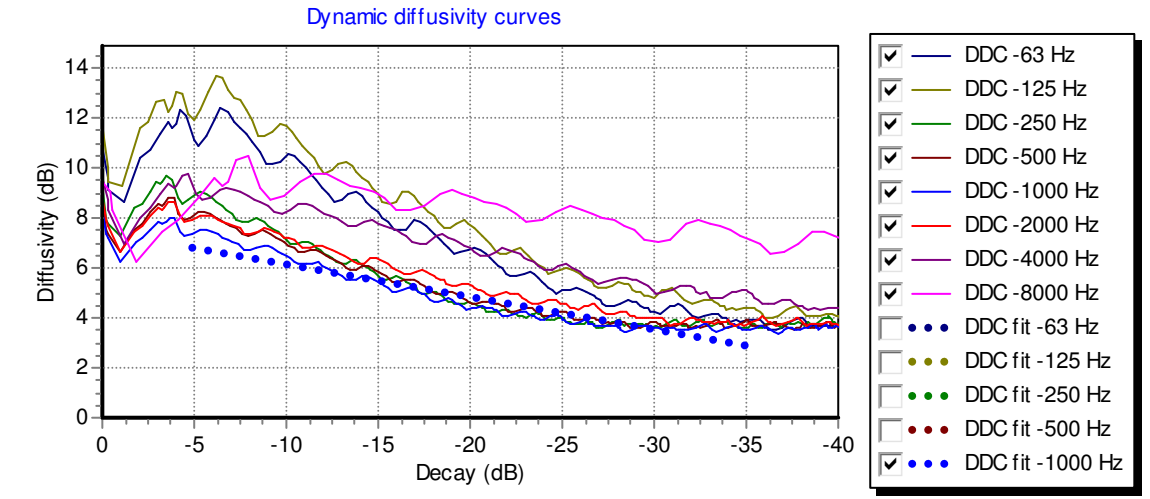
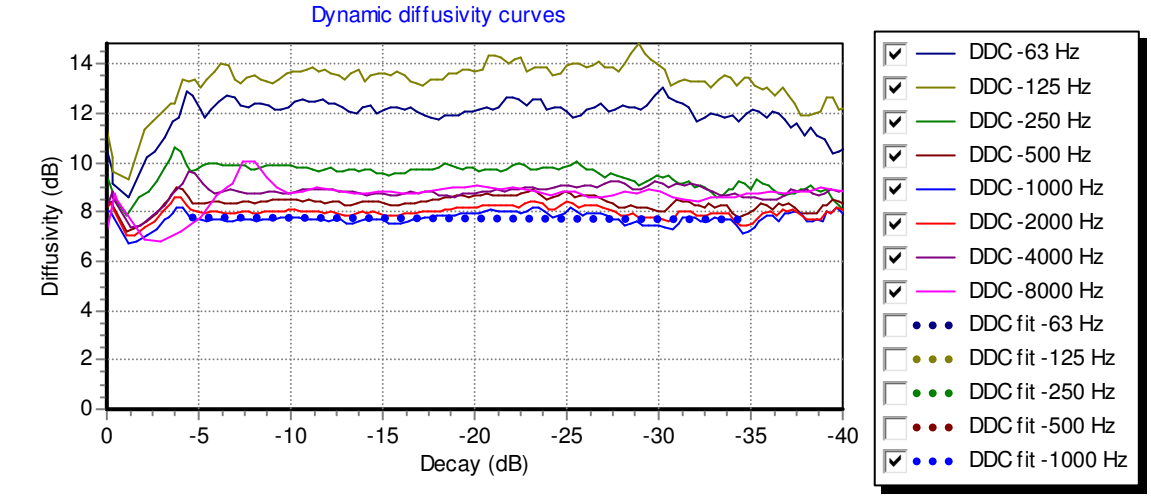


DDC and flutter echo

Before treatment with scattering surfaces



After treatment with scattering surfaces



Conclusions

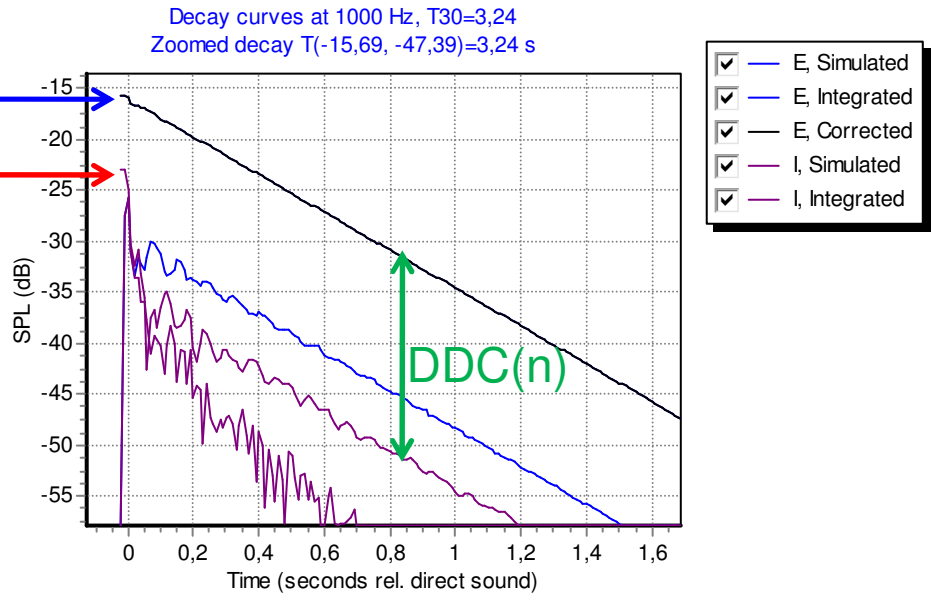
- Dynamic Diffusion Curve DDC is suggested for investigating dynamic behavior of diffusion during decay
- Features for rooms without echoes;
  - Starts with Steady State Diffusion – in auditoria 2-7 dB,
  - Peak value typically within first 5-10 dB of decay
  - Plateau level (rev. diffusion) – in auditoria 5-12 dB
- Features for rooms with echo problems, e.g. flutter echo;
  - Ripples (xx dB?)
- Further research, optimum values, JND's, better tools than DDC?, extract other information from the DDC etc…

Example
Integrated energy and intensity curves

Schröder curve

D(ss)

Backwards integrated
Intensity curve



Integrated energy and intensity curves